

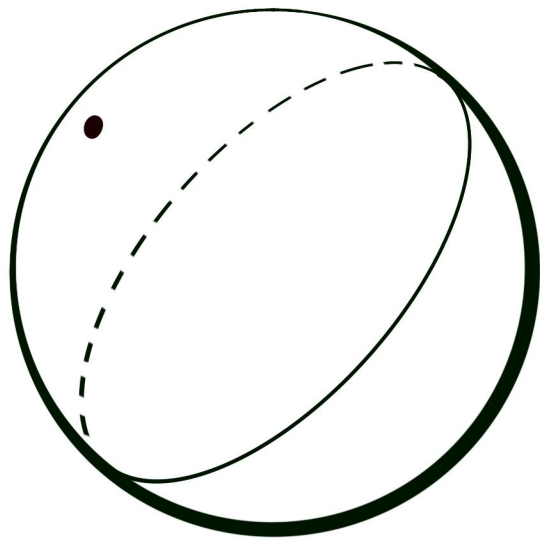
# How To Draw a Sphere

~ a Synthetic, Pencil & eyeball construction ~

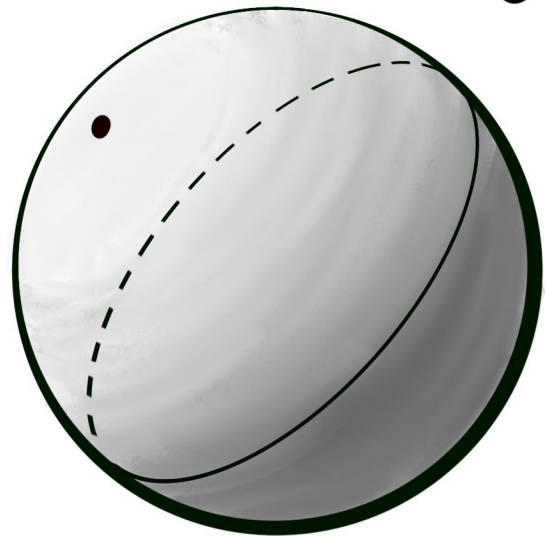


we will break up the process into 4 easy steps

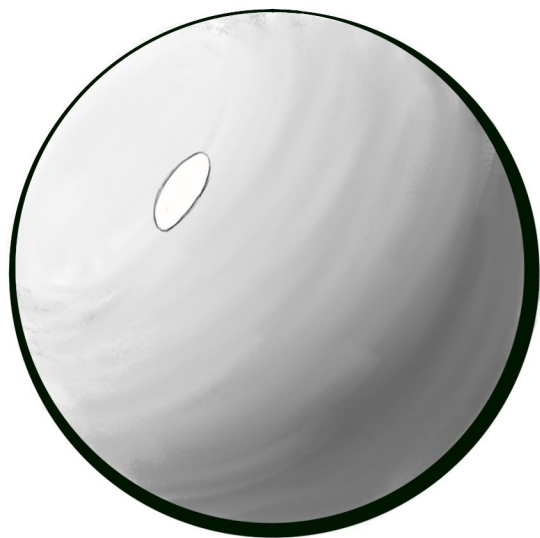
Step 1: Scaffolding



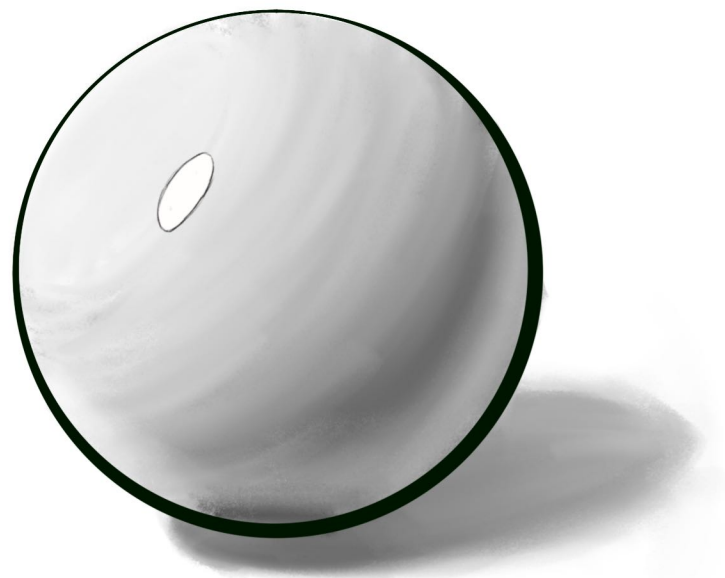
Step 2: shading



Step 3: highlights



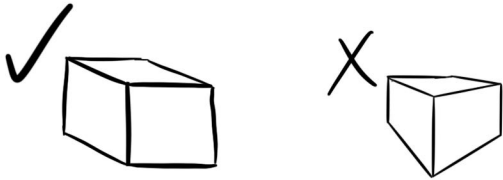
Step 4: Ambiance



**Goal:** draw an unadorned sphere, sitting on a table, in orthographic projection, lit from a sun beam.

Orthographic:

Parallel lines appear parallel



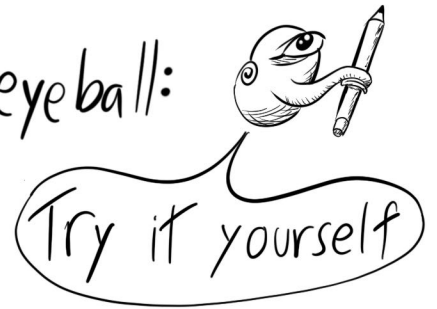
Sunbeam:

All light rays are parallel

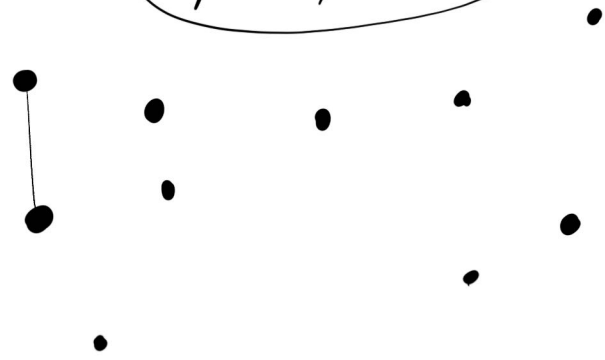


We want to draw this as accurately as possible with no tools except a pencil and our eye. Fortunately, the sphere with all its shadings is exactly constructable. We need to design this construction so that it may be accurately eyeballed. This gives an interesting model of geometry.

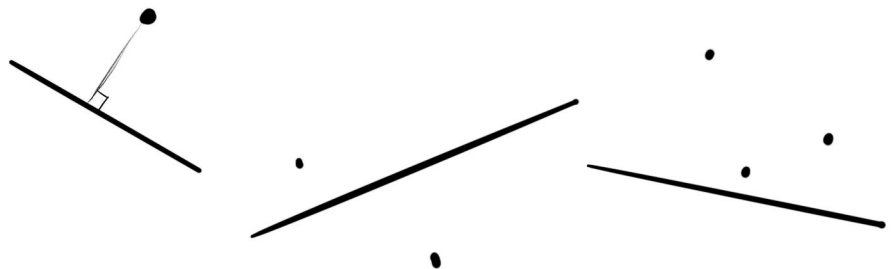
Constructions w/ pencil & eyeball:



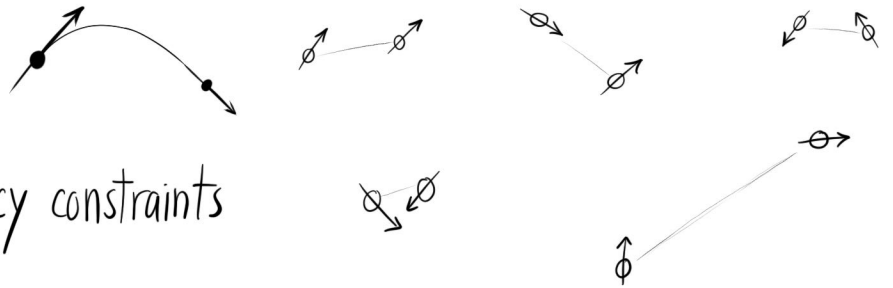
- line between 2 points.  
(can only extend a short distance)



- Perpendicular thru line

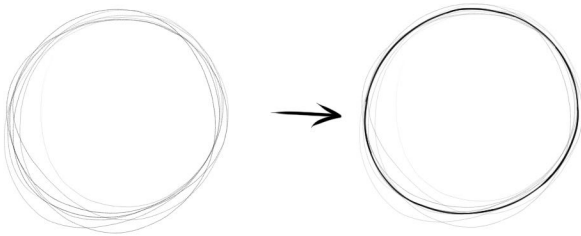


# • Bezier curves



Curves w/ point & tangency constraints

# • Circles



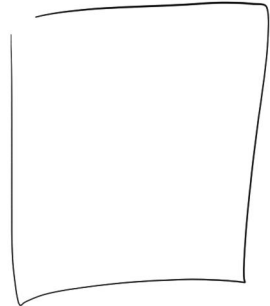
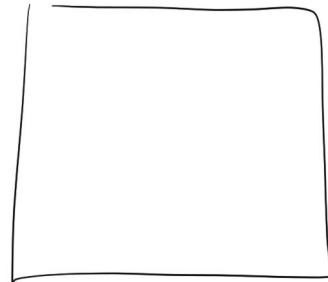
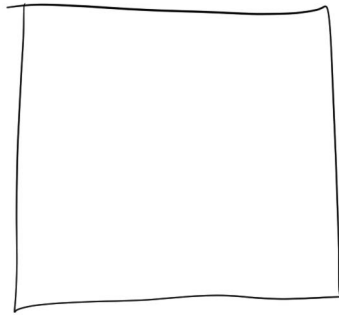
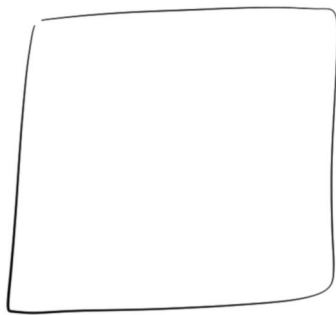
try it!

Tip: How to find lines

- Make many light attempts & see where they concentrate



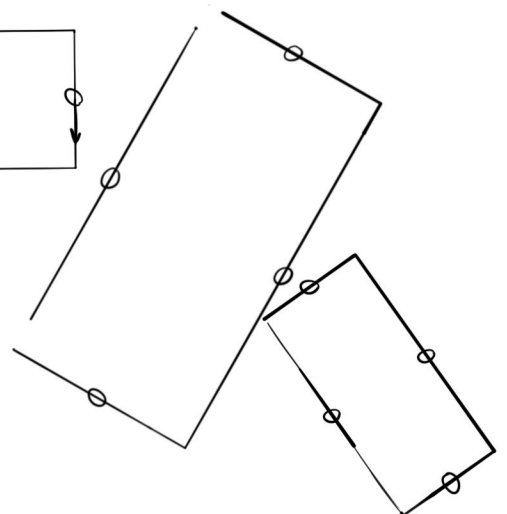
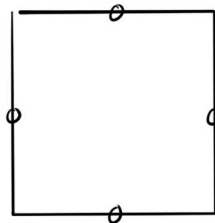
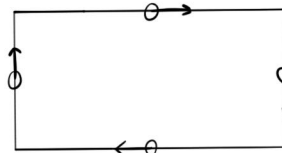
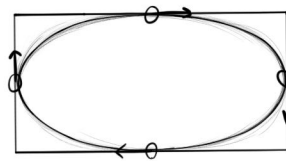
- erase sketch, & make single dark line



or, trace something circular.

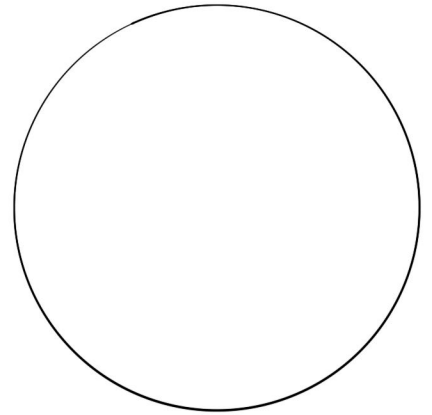
# • Ellipses:

a bunch of Bezier curves does the job



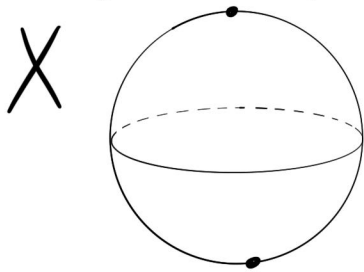
# Step 1: Build the scaffolding

Try to draw a simple diagram of a sphere, showing the equator & north pole:

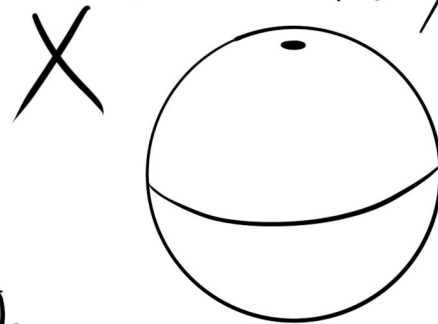


Some common pitfalls:

Seeing both poles at once

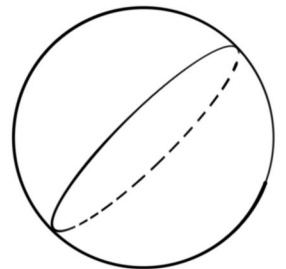
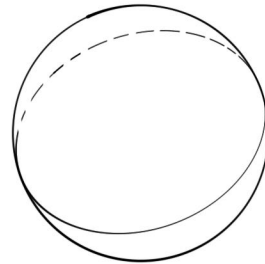
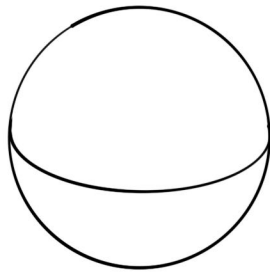


Equator not tangent to boundary

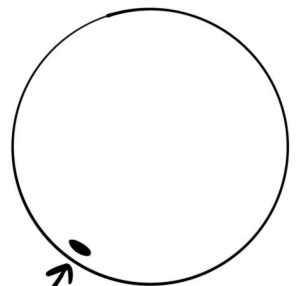
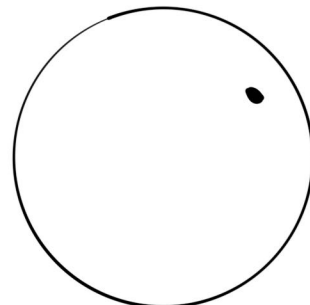
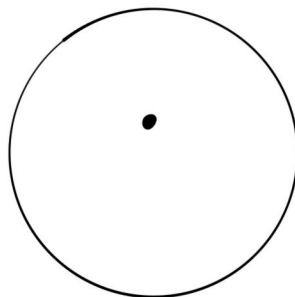


The trickiest part is matching the perspective. The curvature of the equator determines the rotation of the sphere, which determines the pole's position.

Place the poles w/ these equators:



Place the equators w/ these poles:

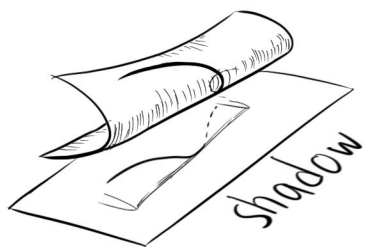
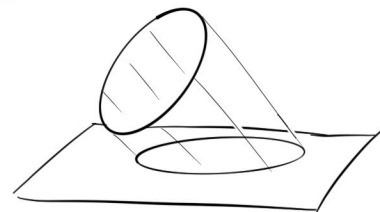


{ Tip: Draw pole as flat disc to show angle

# A theory of equators:



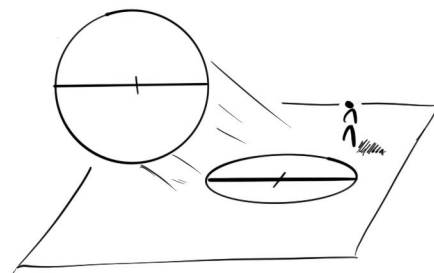
- An equator forms a circle in 3D space, so its projection to the page is an ellipse



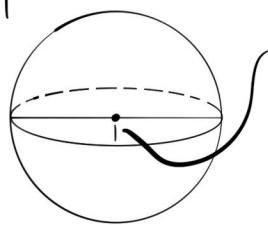
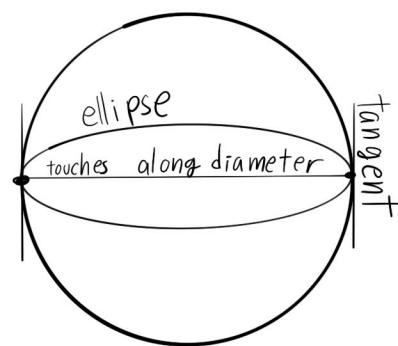
- Any differentiable curve on a surface must project tangent to the folds of the surface

in particular, the equatorial ellipse must be tangent to the outline circle of the sphere

- The major axis of the projection of a circle equals the diameter of the circle. in particular, the equatorial ellipse has major axis equal to the diameter of the outline circle

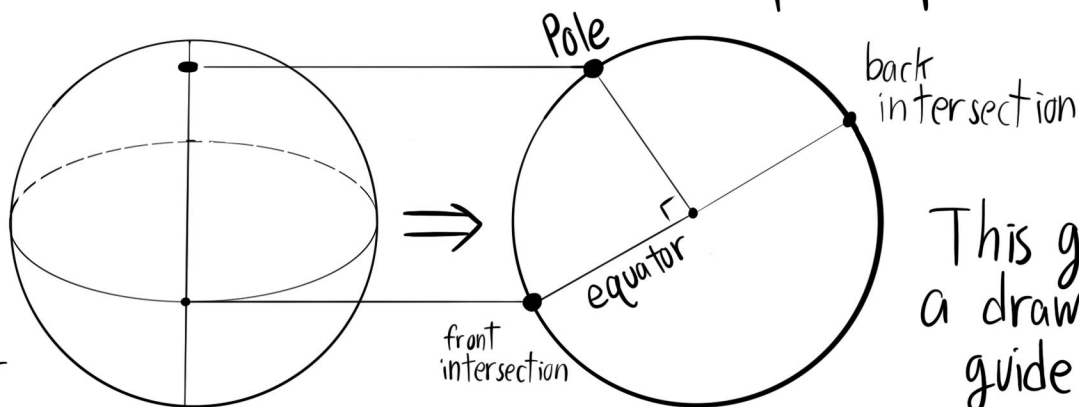


All together, the equator must be drawn as up to rotation of the drawing.



The minor axis controls the perspective so how does minor axis control pole position?

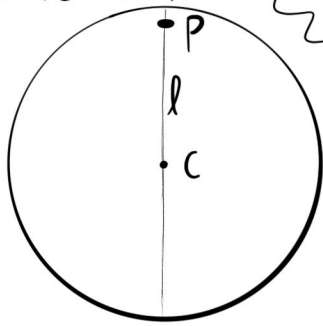
Take a vertical crosssection, & see intersections with pole & equator



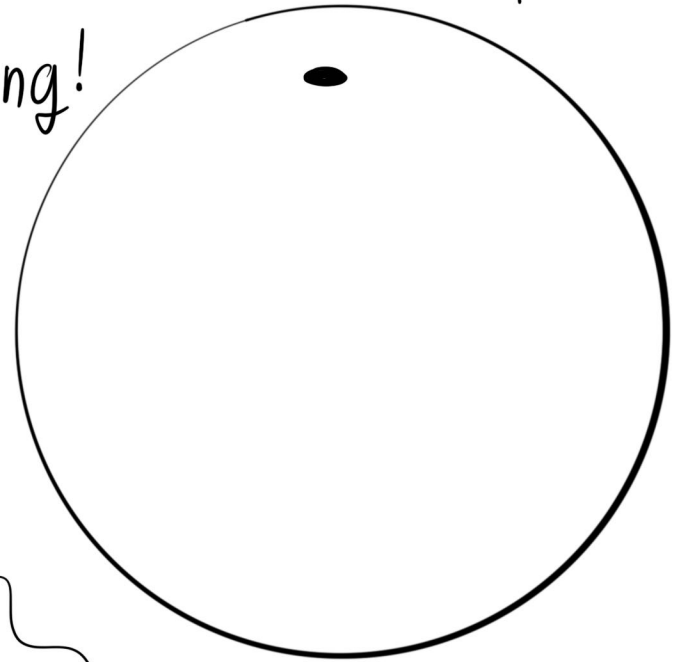
This gives a drawing guide !!

# How to draw an Equator, from the pole

1: Draw line  $l$  from pole to center

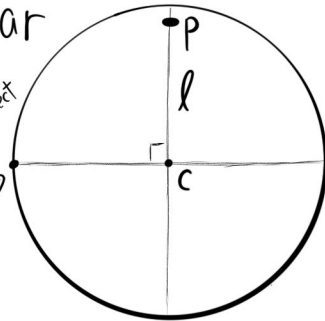


Follow along!



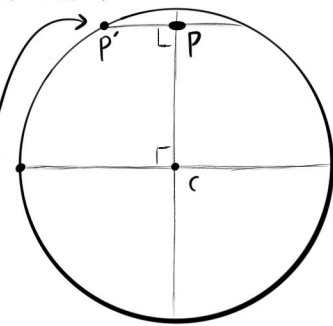
2: Draw perpendicular to  $l$ , from center

this is where equator will intersect boundary



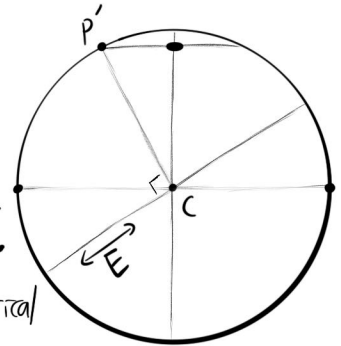
3: Draw perpendicular to  $l$  from pole. intersect w/ outer circle @  $P'$

(we are using the outline circle as our vertical cross-section. This is the pole location)



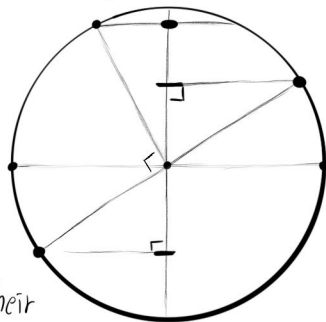
4. Draw line from  $P'$  to center. Construct  $\perp$  through center. Call new line  $E$ .

( $E$  represents equator in the vertical cross-section)

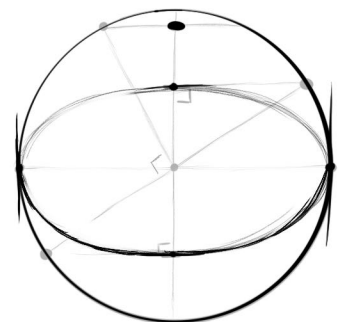


5. Intersect  $E$  with circle, then drop  $\perp$  to  $l$ .

these lines are the vertical extent of the equatorial ellipse. We know the ellipse is tangent to these lines & (by symmetry) the tangency points are their intersection with  $l$ .

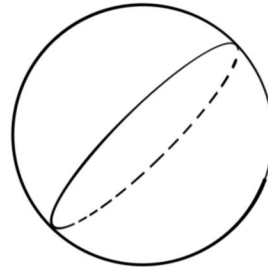
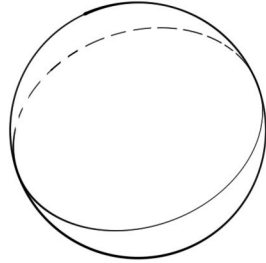
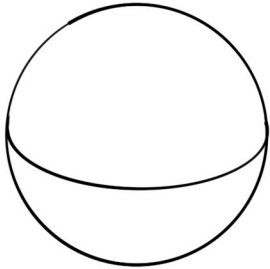
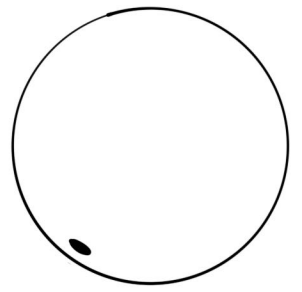
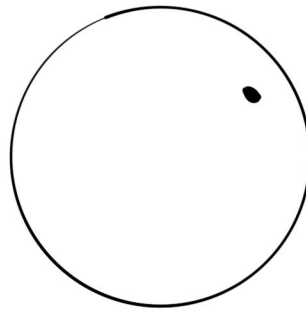
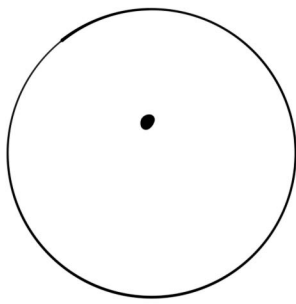


6. construct the equatorial ellipse



# Practice!

Draw equators



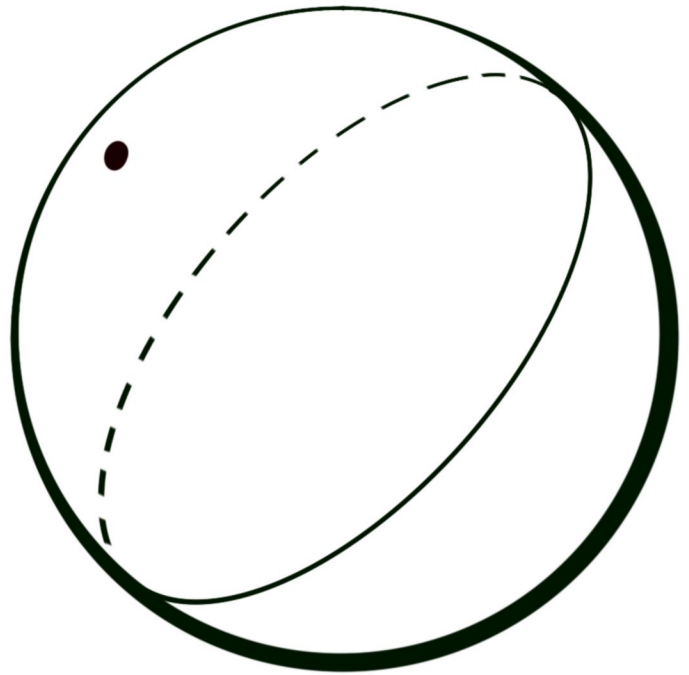
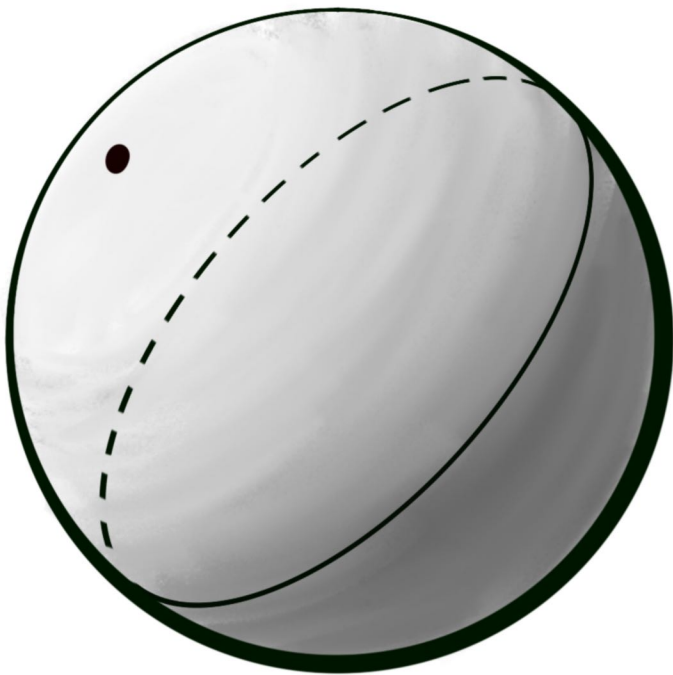
Draw poles

**Shading:** imagine light shining on a sphere, w/ north pole facing towards the light. Everything below equator is facing away, so is in shadow.

- Try to shade:
- Uniform dark color below equator
  - soft gradient above equator, w/ brightest pt @ pole.

Example:

Your turn:



try shading your equators above! on some, put the light behind the sphere.